

# Mathematics

Advanced GCE

Unit **4730**: Mechanics 3

## Mark Scheme for June 2013

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

OCR will not enter into any discussion or correspondence in connection with this mark scheme.

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**Annotations and abbreviations**

<b>Annotation in scoris</b>	<b>Meaning</b>
✓ and ✕	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
^	Omission sign
MR	Misread
Highlighting	
<b>Other abbreviations in mark scheme</b>	<b>Meaning</b>
E1	Mark for explaining
U1	Mark for correct units
G1	Mark for a correct feature on a graph
M1 dep*	Method mark dependent on a previous mark, indicated by *
cao	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working

**Subject-specific Marking Instructions for GCE Mathematics (OCR) Mechanics strand**

- a Annotations should be used whenever appropriate during your marking.

**The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks.** It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

For subsequent marking you must make it clear how you have arrived at the mark you have awarded.

- b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct *solutions* leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly.

Correct but unfamiliar or unexpected methods are often signalled by a correct result following an *apparently* incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, award marks according to the spirit of the basic scheme; if you are in any doubt whatsoever (especially if several marks or candidates are involved) you should contact your Team Leader.

- c The following types of marks are available.

**M**

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, eg by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

**A**

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

**B**

Mark for a correct result or statement independent of Method marks.

4730

## Mark Scheme

### E

A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, eg wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep \*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- e The abbreviation ft implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only — differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, exactly what is acceptable will be detailed in the mark scheme rationale. If this is not the case please consult your Team Leader.

Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

- f Unless units are specifically requested, there is no penalty for wrong or missing units as long as the answer is numerically correct and expressed either in SI or in the units of the question. (e.g. lengths will be assumed to be in metres unless in a particular question all the lengths are in km, when this would be assumed to be the unspecified unit.)

We are usually quite flexible about the accuracy to which the final answer is expressed and we do not penalise over-specification.

### When a value is given in the paper

Only accept an answer correct to at least as many significant figures as the given value. This rule should be applied to each case.

### When a value is not given in the paper

Accept any answer that agrees with the correct value to 2 s.f.

4730

## Mark Scheme

ft should be used so that only one mark is lost for each distinct accuracy error, except for errors due to premature approximation which should be penalised only once in the examination.

There is no penalty for using a wrong value for  $g$ . E marks will be lost except when results agree to the accuracy required in the question.

## g Rules for replaced work

If a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests.

If there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others.

NB Follow these maths-specific instructions rather than those in the assessor handbook.

h For a *genuine* misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A mark in the question.

Marks designated as cao may be awarded as long as there are no other errors. E marks are lost unless, by chance, the given results are established by equivalent working.

'Fresh starts' will not affect an earlier decision about a misread.

Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

## i If a graphical calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers (provided, of course, that there is nothing in the wording of the question specifying that analytical methods are required). Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.

## j If in any case the scheme operates with considerable unfairness consult your Team Leader.

Question	Answer	Marks	Guidance
1	Use of $T = \frac{\lambda e}{l}$  Weight = tension 1 + tension 2  ( $AW =$ ) 1.5 (m)	M1  A1  M1 A1 A1 <b>[5]</b>	Attempt at one tension; allow use of $x$  $\frac{20(d - 0.4)}{0.4}$ or $\frac{30(d - 0.6)}{0.6}$  $100 = 50d - 20 + 50d - 30$  allow $2l$ for M1  either term seen, accept in terms of $x$  condone $Wg$ and $W/g$ fractions and brackets removed
2	(i)	Use of correct formula Vert speed imm before bounce = $2.8 \text{ (ms}^{-1}\text{)}$ Time between bounces = $0.286 \text{ (s)}$ (2/7)	M1 A1 B1 <b>[3]</b>  $v^2 = 0^2 + 2 \times 9.8 \times 0.4$  or by energy
2	(ii)	Use of their $t$ in a correct formula Vert speed imm after bounce = $1.4 \text{ (ms}^{-1}\text{)}$ Coeff of rest = 0.5	M1 A1 B1ft  <b>[3]</b>  $0 = u + 9.8 \times 0.5(t)$ Allow their value of $t$  Their values for $v$ after/ $v$ before  or $-u = u - 9.8t$  must be worked out to fraction or decimal; $0 \leq e \leq 1$
2	(iii)	Imp = change of mom  $I = 1.26 \text{ (Ns)}$	M1  A1 <b>[2]</b>  $I = 0.3 \times (v) + 0.3 \times (u)$ Allow their $u, v$  CAO
3	(i)	Use of $F = ma$  Integrate correctly  $v = \frac{15}{4}t^2 - 5t + 0.8$	M1  A1  A1  <b>[3]</b>  $\frac{3}{2}t - 1 = 0.2 \frac{dv}{dt}$  $v = \frac{15}{4}t^2 - 5t (+c)$  allow sign errors or $m$ omitted  allow if $c$ missing or wrong  oe

Question		Answer	Marks	Guidance
3	(ii)	Use vel = 0.8  $t = 1.33$ (s) or $1 \frac{1}{3}$ (s)	M1 A1 <b>[2]</b>	$\frac{15}{4}t^2 - 5t + 0.8 = 0.8$ must come from correct equation for $v$ ft their (i) Accept 4/3
3	(iii)	Integrate to find $x$ $x = \frac{15}{12}t^3 - \frac{5}{2}t^2 + 0.8t$ Solve for $x = 0$ $t = 1.6$ (s) or $0.4$ (s)	M1* A1  *M1 A1 <b>[4]</b>	At least 2 terms with powers increased by 1 Need to state $c = 0$ , or use limits  Both answers needed; must be from correct work to find equation Ignore $t = 0$
3	(iv)	$x(3) - x(2)$  Distance is 12.05 (m)	M1 A1 <b>[2]</b>	Allow for $x(2)$ or $x(3)$ worked out from (iii) 13.65 or 1.6 Accept 12 or 12.1
4	(i)	Conservation of momentum  Newton's experimental law  Attempt to solve their 2 sim eqns 0.12 in same direction as before	*M1 A1  *M1 A1 M1* A1 <b>[6]</b>	Must have 4 terms $0.1 \times 3 + 0.2 \times 1 \times \cos\theta = 0.1 \times a + 0.2 \times b$ allow sign errors, $\cos\theta$ omitted $a$ and $b$ are vel components of $A$ and $B$ to right, respectively, after collision Must have 4 terms and 0.8 $b - a = -0.8(1 \times \cos\theta - 3)$ allow sign errors, $\cos\theta$ omitted Dep both previous M marks allow 1 slip Direction may be implied by working withhold if direction stated to left
4	(ii)	$b = 2.04$ vel of $B$ perp to line of centres = 0.8 Direction of $B$ after collision makes angle $21.4^\circ$ with line of centres  Angle turned through by $B$ is $31.7^\circ$	B1 B1 M1 A1  A1ft <b>[5]</b>	Must be seen/used in (ii) $(1 \times \sin\theta)$ $\tan\phi = 0.8/2.04$ ; or 0.374 rads or 0.554 rads; allow +/- Allow with their 0.8 and 2.04 ( $b$ from (i)); allow $\tan\phi = 2.04/0.8$ , if angle clear, leading to $68.4^\circ$ for A1 $53.1(3) - \phi$ , $0.927 - 0.374$ rads

Question		Answer	Marks	Guidance
5	(i)	Use of energy equation at $A$ and $B$  $F = ma$ radially  Use of $R = 0$ $\cos TOB = \frac{\sqrt{3}}{3}$ AG	M1  A1 M1 A1 M1 A1  <b>[6]</b>	3 terms needed $mg0.6 \cos \frac{\pi}{6} = mg0.6 \cos \theta + \frac{1}{2}mv^2$  $mg \cos \theta - R = \frac{mv^2}{0.6}$  May be incorporated in previous step Completely correct
5	(ii)	Use of $\sqrt{3}/3$ in 'correct' equation in (i)  1.84 ( $\text{ms}^{-1}$ )	M1  A1  <b>[2]</b>	$mg0.6 \cos \frac{\pi}{6} = mg0.6 \times \frac{\sqrt{3}}{3} + \frac{1}{2}mv^2$  or $mg \frac{\sqrt{3}}{3} = \frac{mv^2}{0.6}$  equation must have gained M1 in (i) but allow restart here
5	(iii)	Use of $F = ma$ tangentially  8.00 ( $\text{ms}^{-2}$ )	M1  A1  <b>[2]</b>	$mg \sin \theta = ma$ seen  allow missing $m/g$ , $-$ sign; allow M1 if angular accel found
6	(i)	Moments about $B$ for equilibrium of $BC$  $W + \sqrt{3}F = R$ AG	M1  A1  <b>[2]</b>	$2Wl \cos 60^\circ + F2l \sin 60^\circ = R2l \cos 60^\circ$  Must be formula for $R$  3 moment terms, condone sin/cos errors and missing $l$ . Need trig terms for M1  correct, with sin/cos evaluated

Question		Answer	Marks	Guidance	
6	(ii)	<p>Moments about A for equilibrium of whole system</p> $W\left(\frac{5\sqrt{3}}{2} + 1\right) + F(\sqrt{3} + 1) = R(\sqrt{3} + 1)$	<p>M1</p> <p>A1</p> <p>A1</p> <p>A1</p> <p>[4]</p>	<p>At least one of <math>F</math> and <math>R</math> terms must involve lengths of both rods</p> <p><math>Wl \cos 30 + 2W(2l \cos 30 + l \cos 60) + F(2l \sin 60 + 2l \sin 30) = R(2l \cos 30 + 2l \cos 60)</math></p> <p>sin/cos left in, but correct</p> <p>fully correct, oe. Mark final answer</p> <p>Allow full credit for candidates who work out internal forces at B and work correctly from there.</p>	<p>At least 3 moment terms, condone sin/cos errors, sign errors and <math>l/2l</math> confusion/missing. Wrong use of forces at B gets M0</p> <p>4 terms, accept sin/cos errors and <math>l/2l</math> confusion/missing and sign errors for A1</p> <p>accept <math>5.33W + 2.73F = 2.73R</math>,  <math>W\left(\frac{13}{4} - \frac{3\sqrt{3}}{4}\right) + F = R</math></p> <p>Eg <math>3R = \sqrt{3}F + 7.5W</math></p>
6	(iii)	<p>Solving 2 sim equations to eliminate <math>F</math> or <math>R</math></p> <p>Use <math>F = \mu R</math> to find <math>\mu</math></p> $(\mu \Rightarrow) \frac{3\sqrt{3}}{13} \quad (0.39970)$	<p>M1</p> <p>A1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>[5]</p>	<p>Both equations must involve <math>W</math>, <math>F</math> and <math>R</math></p> <p><math>F = \frac{3\sqrt{3}}{4}W</math></p> <p><math>R = \frac{13}{4}W</math></p> <p>At any point</p> <p>Or eliminate <math>W</math> M1A1A1        Use <math>F = \mu R</math> M1        cao A1</p> <p>allow slips in working</p> <p><math>F = 1.299 W</math></p> <p><math>R = 3.25 W</math></p> <p>Accept 0.4 if with correct working  <math>5.33(R - 1.73F) + 2.73F = 2.73R</math>  <math>2.6R = 6.52F</math></p>	

Question		Answer	Marks	Guidance
7	(i)	Use of $F = ma$ when string stretched  Show $x = 1$ is centre of SHM or that $x = 1$ is equilibrium position.	M1  A1  B1  [3]	Must have $mg -$ tension term (involving $39.2m, 0.8$ and $x$ ) = $ma$ $mg - \frac{39.2m(x-0.8)}{0.8} = m\ddot{x}$ $\ddot{x} = -49(x-1)$  and state about $x = 1$
7	(ii)	By energy  $e = 0.8$ satisfies this equation <b>AG</b>	M1  A1  A1  [3]	Must be PE term and EE term $mg(0.8+e) = \frac{39.2me^2}{2 \times 0.8}$  Or by solving quadratic in $e$ Allow full credit if done correctly from $v^2 = \omega^2(a^2 - x^2)$

allow if sign errors;  $x$  could be length or ext of string, or from eq<sup>m</sup> pos.

$$mg - \frac{39.2mx}{0.8} = m\ddot{x} \text{ leads to}$$

$$\ddot{x} = -49(x-0.2)$$

$$mg - \frac{39.2(x+0.2)}{0.8} = m\ddot{x} \text{ leads to}$$

$$\ddot{x} = -49x$$

Convincingly

Allow for missing '2', wrong 'g' or inconsistent lengths

$$\text{Or } mgh = \frac{39.2m(h-0.8)^2}{2 \times 0.8} \text{ and}$$

$$h = 0.8 + e$$

$$2.5e^2 - e - 0.8 = 0$$

Convincingly

Allow integration of  $v \frac{dv}{dx} = g - 49x$

Question		Answer	Marks	Guidance
7	(iii)	For SHM, $\omega = 7$ $a = 0.6$ Correct use of appropriate SHM distance equation $t = 0.272(9476)$ from bottom ( $x = 1.6$ ) to $x = 0.8$ $t = 0.404(061)$ from $O$ to $x = 0.8$  Time to reach lowest point = $0.677$ s	B1 B1 M1 A1 B1 A1ft <b>[6]</b>	To be awarded if seen in (i) or (iv) or seen or used here Allow $+0.2$ , allow their $a$ and $\omega$  Could be $0.0485 + 0.224$  Or $\frac{2\sqrt{2}}{7}$ (‘0.273’ + ‘0.404’)
7	(iv)	Use of $v = -a\omega\sin\omega t$ or $a\omega\cos\omega t$ $v = -0.6 \times 7\sin 7t$ Use of $t = 0.8 - 0.677 = 0.123$ after bottom point $v = 3.19$ (3.185677...)	M1 A1 B1ft A1  <b>[4]</b>	Must fit from their ‘x’ equation in (iii), or shown here or $0.6 \times 7\cos 7t$ Or use of $t = 0.3475$ in ‘cos’ version  Allow use of their $a$ and $\omega$ , sign error  Must be between 0 and 0.8  Do not allow if direction stated to be down.

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